Seat No.:	Enrolment No
GUJARAT TECHNOLOGI BE - SEMESTER-I & II(NEW) EXAM	
Subject Code:3110015	Date:14-03-2023
<b>Subject Name: Mathematics - 2</b>	C
Time:10:30 AM TO 01:30 PM	Total Marks:70
Instructions: 1. Attempt all questions. 2. Make switchle assumptions wherever passesses.	co°

- 2. Make suitable assumptions wherever necessary.
- 3. Figures to the right indicate full marks.
- 4. Simple and non-programmable scientific calculators are allowed.

- If  $\overline{F} = 2xyz\hat{\imath} + (x^2z + 2y)\hat{\jmath} + x^2y\hat{k}$  then
  - If  $\overline{F}$  is conservative, find its scalar potential  $\emptyset$ .
  - Find the work done in moving a particle under this force field from (0,1,1) to (1,2,0).

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O-3Find the constant b such that 3  $\overline{A} = (bx + 4y^2z)\hat{\imath} + (x^3sinz - 3y)\hat{\jmath} - (e^x + 4cosx^2y)\hat{k} \text{ is solenoidal.}$ (b) Evaluate  $\int_0^\infty te^{-2t} cost dt$ . (c) By Laplace transform solve,  $\frac{dy}{dt} + y = \cos 2t$ , y(0) = 1. 7

- Q-3 State Second Shifting theorem. Hence find the inverse Laplace transform of  $\frac{e^{-as}}{s}$ . 3
  - Solve  $\frac{dy}{dx} + \frac{1}{x} = \frac{e^y}{x^2}$ . 4
  - (i) Solve  $y = 2px xp^2$ (ii) Solve p = log(px y)7 (c)

- Q-4 (a) If  $y_1 = e^{-x}$  is one of the solutions of y'' + 2y' + y = 0, then find the second solution.
  - (b) Solve  $(D^2 2D + 1)y = 10e^x$ .
  - (c) Find the solution of differential equation y'' + 4y = 2sin3x by the method of Undetermined Coefficients.

OR

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- Q-4 (a) Solve  $2D^2y + Dy 6y = 0$ .
  - (b) Solve  $(x^2D^2 7xD + 12)y = x^2$ .
  - Using the method of variation of parameter, solve  $\frac{d^2y}{dx^2} + y = sinx$ .
- Q-5 (a) Find the ordinary points of  $(x^2 + 1)\frac{d^2y}{dx^2} + 2x\frac{dy}{dx} + 6y = 0$ 
  - (b) Solve  $(D^2 + 1)y = \sin^2 x$ .
  - (c) Find power series solution of  $\frac{d^2y}{dx^2} + xy = 0$ .
- Q-5 (a) Find the value of  $J_{\frac{3}{2}}(x)$ .
  - (b) Find the Laplace transform of  $f(t) = \frac{2}{3}t$ ,  $0 \le t \le 3$ , if f(t) = f(t+3).
  - (c) Solve in series the differential equation  $4x \frac{d^2y}{dx^2} + 2y \frac{dy}{dx} + y = 0.$