$\qquad$
$\qquad$

# GUJARAT TECHNOLOGICAL UNIVERSITY <br> MCA - SEMESTER- III• EXAMINATION - WINTER 2020 

Subject Code:4639301
Date:08/01/2021
Subject Name:Basic Mathematics
Time:10:30 AM to 12:30 PM
Total Marks: 56
Instructions:

1. Attempt any FOUR questions out of EIGHT questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
Q. 1 (a) Define the following terms:
I) Subset
II) Cardinality number of a set
III) Singleton set
IV) Reflexive Relation
V) Function
VI) Null Graph
VII) Binary Tree
(b) Check the validity of the following argument using predicates, quantifiers and logical connectives:
All humans are mortal.
Socrates is a human.
Therefore, Socrates is mortal.
Q. 2 (a) Give a Direct proof to show that, the sum of two odd integers is an even integer. 07
(b) I) Let the two matrices $A=\left[\begin{array}{ccc}1 & 2 & -3 \\ 3 & 7 & 5 \\ 0 & 1 & 12\end{array}\right]$ and $B=\left[\begin{array}{ccc}8 & 6 & 3 \\ 2 & 4 & 1 \\ 0 & -1 & 9\end{array}\right]$.Compute
$A+B, A-B \& B^{T}$.
II) Find the power set of the following sets:
(i) $A=\{r, s, t\}$
(ii) $\mathrm{B}=\{\phi,\{\phi\}\}$
Q. 3 (a) Using Euclidean Algorithm $(a=b q+r)$, find the GCD of the integers, $a=227407$ \& $b=174$. Also find the LCM of these integers.
(b) I) Prove by Mathematical induction," 5 divides $5 n+3$ for all positive integers $n$ ". $\mathbf{0 3}$
II) Prove that the statement formula $[p \wedge(p \rightarrow q)] \rightarrow q$ is tautology, using the 04 truth table.
Q. 4 (a) Convert $(3 F B 09)_{16}$ from hexadecimal to decimal representation.
(b) I) Prove by Mathematical induction: " $7^{n}+5$ is divisible by 3 for all integers $n \geq 0$ ".
II) Give the converse, inverse and contrapositive of the implication:
"If it is raining, then I get wet".
Q. 5 (a) The relation R from the set $\mathrm{A}=\{2,5,7,18\}$ into the set $\mathrm{B}=\{2,3,4,5,10\}$ is defined by $a \mathrm{R} b$ if and only if $a \leq b$. Write the relations R and $R^{-1}$ as a set of ordered pairs. Write the matrix of $R$. Also find the domain and range of the relation R .
(b) Define one-one and onto function. Let $f: A \rightarrow B$ be the function from the set $\mathrm{A}=\{3,4,5,6,7,8\}$ into the set $\mathrm{B}=\{0,1,2,3,4\}$, given by $f=\{(3,4),(4,1),(5,3)$, $(6,0),(7,2),(8,4)\}$. Check whether the function $f$ is one-one (injective) or onto (surjective) or both.
Q. 6 (a) Give the definition of an equivalence relation. Prove that the given relation R on the set $\mathrm{A}=\{1,2,3,4\}$ is an equivalence relation. Here, $\mathrm{R}=\{(1,1),(1,2),(2,1)$, $(2,2),(3,3),(3,4),(4,3),(4,4)\}$.
(b) Define composition of functions. Let the functions $f: R \rightarrow R \& g: R \rightarrow R$ be defined by $f(x)=4 x-3$ and $g(x)=x^{2}+2, \forall x \in R$. Find gof,$f o f \& g o g$.
Q. 7 (a) Define a directed graph (digraph). Write the adjacency matrix of the below directed graph. Also discuss the in degree and out degree of each node (vertex) from the matrix. Is there any isolated node in the graph?

(b) Is the given tree a Binary tree? Also determine the order in which the nodes will be visited if the tree is traversed in Inorder , Postorder and Preorder.

Q. 8 (a) Check whether the below graph is weakly, unilaterally or strongly connected. If it is not fall any of the above categories then find its components.

(b) Represent the below tree in Parenthesized expression and in List of content of a book expression (Index)

