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## GUJARAT TECHNOLOGICAL UNIVERSITY <br> ME - SEMESTER - I (New)- EXAMINATION - WINTER-2019

Subject Code: 3710812
Date: 02-01-2020

## Subject Name: Computational Method for Mechanical Engineering <br> Time: 02:30 PM TO 05:00 PM <br> Total Marks: 70

## Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
Q. 1 (a) There is a system for the unknown currents $i_{1}, i_{2}$ and $i_{3}$ in the electrical network. Using Kirchhoff's current and voltage laws the following equations obtained. Find the current using Gauss elimination method.

$$
i_{1}-i_{2}+i_{3}=0,-i_{1}+i_{2}-i_{3}=0,10 i_{2}+25 i_{3}=90,20 i_{1}+10 i_{2}=80
$$

(b) Solve the following initial-value problem arises from a mechanical system using Laplace transform

$$
y^{\prime \prime}+3 y^{\prime}+2 y=e^{t}, y(0)=1, y^{\prime}(0)=0
$$

Q. 2 (a) It has been claimed that in $60 \%$ of all solar-heat installations the utility bill is reduced by at least one-third. Accordingly, what are the probabilities that the utility bill will be reduced by at least one-third in
(i) Four of five installations
(ii) At least four of five installations?
(b) Find the Fourier series of $f(x)=x^{2}$ in the interval $(0,2 \pi)$ and hence deduce that $\frac{\pi^{2}}{12}=\frac{1}{1^{1}}-\frac{1}{2^{2}}+\frac{1}{3^{2}}-\cdots$

OR
(b) Derive the governing ordinary differential equation for the damped vibration and discuss all the cases.
Q. 3 (a) If P is the pull required to lift a load W by means of a pulley block, find a linear law of the form $\mathrm{P}=\mathrm{mW}+\mathrm{c}$ connecting $\& \mathrm{~W}$ using following data,

| P | 12 | 15 | 21 | 25 |
| :--- | :--- | :--- | :--- | :--- |
| W | 50 | 70 | 100 | 120 |

Where P and W are taken in Kgs . \& compute P when $\mathrm{W}=150 \mathrm{Kgs}$.
(b) The velocity of a train which starts from rest is given by the following table, the time being reckoned in minutes from the start and speed in $\mathrm{Km} / \mathrm{hrs}$.

| Time (minutes) | 0 | 3 | 6 | 9 | 12 | 15 | 18 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Velocity(kms/hr) | 0 | 22 | 29 | 31 | 20 | 04 | 00 |

Estimate approximately the distance covered in 18 minutes by simpson's $3 / 8$ rule OR
Q. 3 (a) A practical study was carried out to check the effect of parameters on various
properties of sand mold collected data are as follows,

| Water content | Mold hardness <br> $\left(\mathrm{Kg} /(\mathrm{cm})^{2}\right)$ | Permeability | Shear <br> stress $\left(\mathrm{Kg} /(\mathrm{cm})^{2}\right)$ |
| :--- | :--- | :--- | :--- |
| $3 \%(15 \mathrm{ml})$ | 91 | 210 | 0.38 |
| $4 \%(20 \mathrm{ml})$ | 86 | 300 | 0.50 |
| $5 \%(25 \mathrm{ml})$ | 83 | 360 | 0.55 |
| $6 \%(30 \mathrm{ml})$ | 78 | 380 | 0.88 |

Compute the values of mold hardness when water content is $4.5 \%$ using newton's forward interpolation.
(b) (1) Determine a $90 \%$ confidence interval foe the mean of a normal distribution
with variance $=16$, using a sample of $\mathrm{n}=100$, with mean $=8$. Take corresponding value of c from below table.

| $\gamma$ | $90 \%$ | $95 \%$ | $99 \%$ | $99.9 \%$ |
| :--- | :--- | :--- | :--- | :--- |
| c | 1.645 | 1.960 | 2.576 | 3.291 |

(2) A random variable X has the following probability distribution

| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{P}(\mathrm{X})$ | a | 4 a | 3 a | 7 a | 8 a | 10 a | 6 a | 9 a |

(i) Find the value of a.
(ii) Find $\mathrm{P}(\mathrm{X}<3)$
Q. 4 (a) A tightly stretched string with fixed end points at $x=0$ and $x=20$ is initially given the deflection $f(x)=k x(20-x)$. If it is released from this position, then find the deflection of the string.
(b) Find the dominant eigen value of $\mathrm{A}=\left[\begin{array}{ll}1 & 2 \\ 3 & 4\end{array}\right]$ by Power method by choosing $x_{0}=[1,1]^{T} \&$ hence find the other eigen value also.

## OR

Q. 4 (a) A rod of length 1 with insulated side is initially at uniform temperature $100^{\circ} \mathrm{C}$.

Its ends are suddenly cooled at $0^{\circ} \mathrm{C}$ and kept that temperature. Find the temperature $u(x, t)$.
(b) If $\vec{F}=\left(2 x^{2}-4 z\right) \hat{\imath}-2 x y \hat{\jmath}-8 x^{2} \hat{k}$ then evaluate $\iiint_{V} \operatorname{div} \vec{F} d v$, where V is07 bounded by the planes $x=0, y=0, z=0$ and $x+y+z=2$
Q. 5 (a) Verify Green's theorem for $\oint_{c}[(x-y) d x+3 x y d y]$ where $c$ is the boundary of07 the region bounded by the parabolas $x^{2}=4 y$ and $y^{2}=4 x$.
(b) Solve the differential equation using method of variation of parameter

$$
y^{\prime \prime}-7 y^{\prime}+6 y=2 \sin 3 x
$$

## OR

Q. 5 (a) Solve the differential equation : $y^{\prime \prime}-y=t ; \quad y(0)=y^{\prime}(0)=1$.07
(b) Find the eigenvalues and corresponding eigenvectors of the matrix

$$
\left[\begin{array}{ccc}
4 & 0 & 1 \\
-2 & 1 & 0 \\
-2 & 0 & 1
\end{array}\right]
$$

