

**GUJARAT TECHNOLOGICAL UNIVERSITY**

**ME – SEMESTER – II (New)– EXAMINATION – WINTER-2019**

**Subject Code: 3720801**

**Date: 25-11-2019**

**Subject Name: Finite Element Analysis**

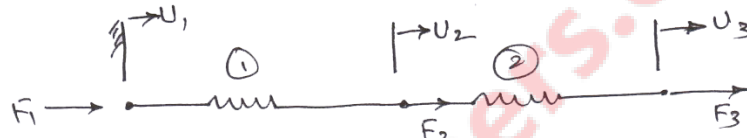
**Time: 02:30 PM TO 05:00 PM**

**Total Marks: 70**

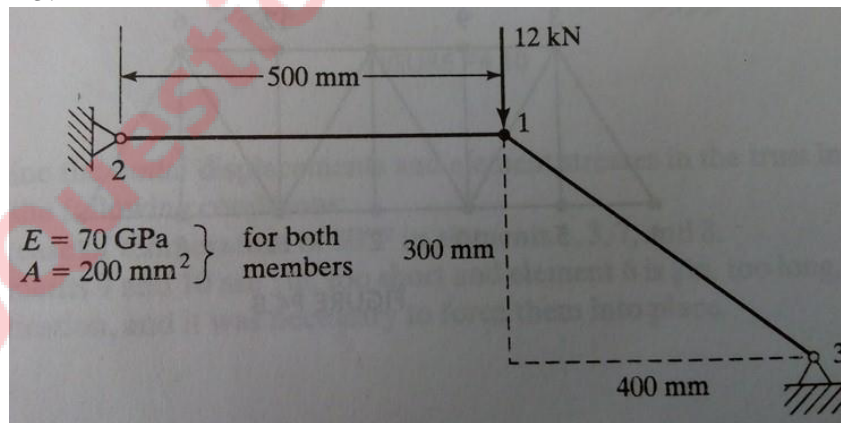
**Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1 (a)** Write comparison of Finite Element and Finite difference methods. Giving suitable example, explain Lagrange’s method for a three degree of freedom spring mass system. Get the required equations of motion **07**
- (b)** Explain in brief: “Free body diagrams of elements and nodes” of below given figure. Also derive K matrix **07**

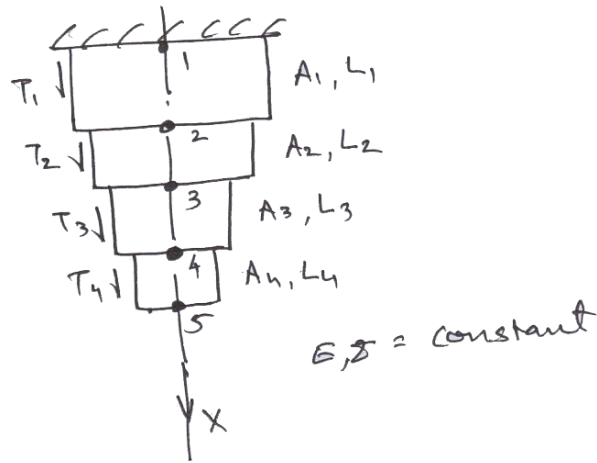


- Q.2 (a)** Giving suitable example, explain Lagrange’s method for a three degree of freedom spring mass system. Get the required equations of motion. **07**
- (b)** For the two bar truss shown below figure, determine the displacements of node 1 and stress in element 1-3. **07**



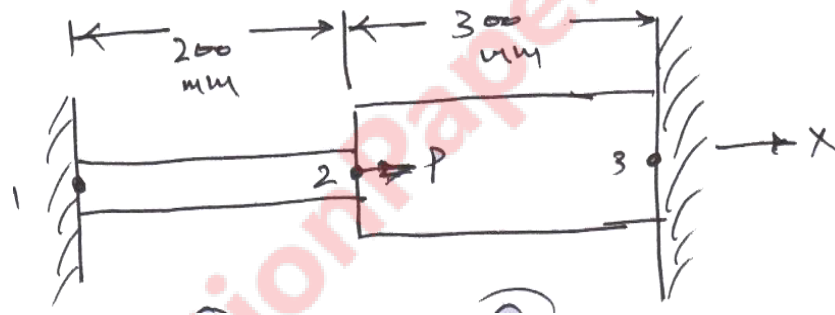
**OR**

- (b)** Consider the bar shown below. **07**  
 For each element  $i$ ,  $A_i$  and  $l_i$  are the cross sectional area and length respectively. Each element  $i$ , subjected to a traction force  $T_i$ , per unit length and body force  $f$  per unit volume. The units of  $T_i$ ,  $f$ ,  $A_i$  and so on are assumed to be consistent. The Young’s modulus of the material is  $E$ . A concentrated load  $P_2$  is applied at node 2. Derive step by step structured stiffness matrix and nodal load vector



**Q.3 (a)** In axial load  $p = 300 \times 10^3 \text{N}$  is applied at  $20^\circ\text{C}$  to the rod as shown below. The temperature is then raised to  $60^\circ\text{C}$ . Assemble L and F matrices and determine the nodal displacement and element stress. **07**

(1)	(2)
Aluminum	Steel
$E = 70 \times 10^9 \text{N/m}^2$	$200 \times 10^9 \text{N/m}^2$
$A = 900 \text{mm}^2$	$1200 \text{mm}^2$
$X = 23 \times 10^{-6} \text{ per } ^\circ\text{C}$	$11.7 \times 10^{-6} \text{ per } ^\circ\text{C}$



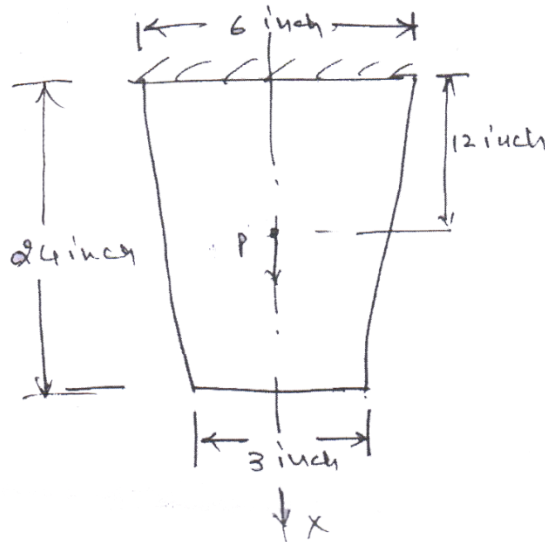
**(b)** Differentiate the following **07**  
 (i) Transient and Eigen value problems  
 (ii) Completeness and compatibility of elements

**OR**

**Q.3 (a)** Consider the thin plate as below: **07**  
 The plate has a uniform thickness  $t=1$  inch. Having Young's modulus  $E = 30 \times 10^6 \text{psi}$  and weight density  $\rho = 0.2836 \text{lb/in}^3$ . The plate is subjected to a point load  $P = 100 \text{lb}$  at its midpoint.

Find:

- Model the plate and write expression for the stiffness matrices and element body force vectors.
- Assemble the structural stiffness matrix  $K$  and global load vector  $F$ .
- Using elimination approach, solve the global displacement vector  $Q$
- Evaluate the stresses in each element
- Determine the reaction force at the support



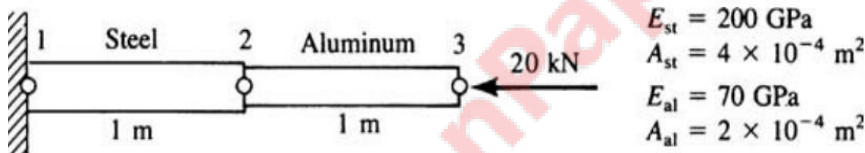
(b) Discuss the shape function for 4-node quadrilateral element and define isoparametric formulation. 07

**Q.4 (a)** The quality of the result of FEA mainly depends upon the type of elements selected, size of the element and number of elements. Justify the statement giving examples. 07

(b) Explain the “procedure to model the object” with reference to a FEA software. Also explain in brief: i) Preprocessing ii) Solution iii) Post Processing 07

**OR**

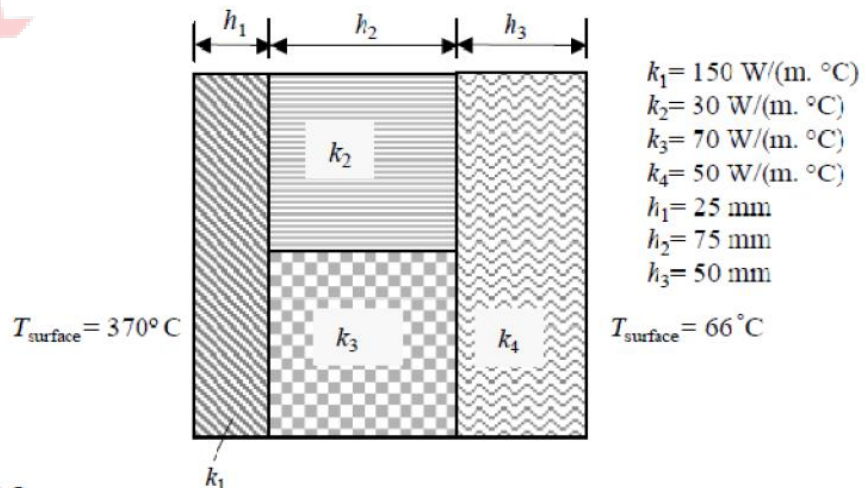
**Q.4 (a)** Determine nodal displacement and stresses in each elements for the bar assemblage in the below figure. 07



(b) Explain following terms: (1) Sub-parametric formulation (2) Super parametric formulation (3) Mass lumping 07

**Q.5 (a)** Discuss the effect of node numbering. Also differentiate between Kirchoff plate and Mindlin plate elements in terms of their capabilities and limitations. 07

(b) Find the heat transfer per unit area through the composite wall shown below. Assume one dimensional heat flow. 07

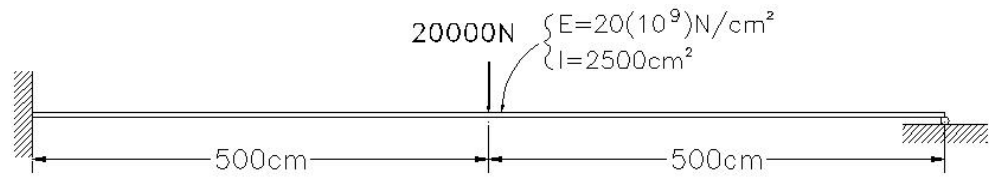


**OR**

**Q.5 (a)** Explain the terms Plane Stress and Plane Strain. Explain how will you solve a plane stress problem using FEA software. 07

- (b) A beam fixed at one end and supported by a roller at the other end, has a 20 kN concentrated load applied at the center of the span (Figure 5). Calculate the deflections under the load .

07



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